

$$\int x^n dx = \frac{x^{n+1}}{n+1} \quad (n \neq -1)$$

$$\int e^x dx = e^x$$

$$\int \sin x dx = -\cos x$$

$$\int \sec^2 x dx = \tan x$$

$$\int \sec x \tan x dx = \sec x$$

$$\int \sec x dx = \ln |\sec x + \tan x|$$

$$\int \tan x dx = \ln |\sec x|$$

$$\int \sinh x dx = \cosh x$$

$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}$$

$$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x - a}{x + a} \right|$$

$$\int \frac{1}{x} dx = \ln |x|$$

$$\int a^x dx = \frac{a^x}{\ln a}$$

$$\int \cos x dx = \sin x$$

$$\int \csc^2 x dx = -\cot x$$

$$\int \csc x \cot x dx = -\csc x$$

$$\int \csc x dx = \ln |\csc x - \cot x|$$

$$\int \cot x dx = \ln |\sin x|$$

$$\int \cosh x dx = \sinh x$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}, \quad a > 0$$

$$\int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln \left| x + \sqrt{x^2 \pm a^2} \right|$$

# Strategy for Integration

## 1. Simplify the Integrand if Possible

- Try algebraic manipulations or trigonometric identities.

## 2. Look for an Obvious Substitution

- Try to find a  $u = g(x)$  such that  $du = g'(x)dx$  also occurs.

## 3. Classify the Integrand According to Its Form

- (a) *Trigonometric functions*, use substitutions or half-angle formulas
- (b) *Rational functions*, use division and partial fractions
- (c) *Integration by parts*, look for products according to the LIATE rule
- (d) *Radicals*
  - (i)  $\sqrt{\pm x^2 \pm a^2}$  - use trigonometric substitution
  - (ii)  $\sqrt[n]{ax + b}$  - use rationalization substitution  $u = \sqrt[n]{ax + b}$

# Strategy for Integration

## 4. Try Again

- (a) *Try substitution*, including non-obvious ones
- (b) *Try parts*, e.g. on single functions such as  $\ln x$
- (c) *Manipulate the integrand*, like in step 1. but more substantial
- (d) *Relate the problem to previous problems*, remember previously calculated integrals and previously used tricks
- (e) *Use several methods*, such as several substitutions, or substitutions and integration by parts